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Reviewer's Discussion

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Effects of Restitution in the Application of Crush Coefficients

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The authors' revised model for restitution takes a step in the right direction. The revised model, however, is not entirely realistic. As a result, it may not correctly represent a vehicle's crush response characteristics.

The revised model for restitution in figure 6A is a completely elastic crush response ($\epsilon=1.0$) through the first several inches of dynamic crush. Completely elastic dynamic crush is a theoretical condition. In the real world, restitution may approach the theoretical magnitude of 1.0 but will never equal 1.0. Restitution is a mathematical "limit." The limit of the magnitude of restitution is 1.0 as dynamic crush approaches zero. Therefore, it is not realistic for the first several inches of dynamic crush to be completely elastic. In addition, the revised equation for restitution (appendix 1, equation 1) is an "infinite limit," or asymptote, where restitution (ϵ) becomes infinite as dynamic crush (δ_m) approaches zero. This equation is not realistic. If this model is implemented in a computer program, hopefully the program will provide the necessary limit not present in equation (1).

The crush response of the high restitution hypothetical vehicle in figure 2 is completely elastic through the first 6.2 inches of crush. A completely elastic crush response ($\epsilon=1.0$) through the first 6.2 inches of crush is not realistic. Clearly front bumpers, with rare exception, do not extend 6.2 inches beyond easily damaged vehicle components such as the fenders and hood (note: any residual damage means $\epsilon \neq 1.0$). Also "energy absorbing" bumpers that are present on vehicles "absorb energy" and, therefore, are not completely elastic. In addition, the vehicle in figure 2 would begin to develop residual crush ($\epsilon < 1.0$) after the first 5.6 inches of dynamic crush. This means that, between 5.6 inches and 6.2 inches of dynamic crush, the vehicle's crush response is partially plastic ($\epsilon < 1.0$) yet at the same time is completely elastic ($\epsilon=1.0$). This is impossible.

Considering the above, the conclusions and graphs that are drawn from analyzing the hypothetical vehicles are subject to question (Analytical Approach section, figures 4 & 5). If the revised restitution model can produce a vehicle that could not exist in the real-world, can one be certain that the revised coefficients will correctly represent a vehicle's crush response characteristics when applied to a real-world vehicle?

Figure 2 Calculations:

Use equation (1), set $\epsilon=1.0$ and solve for δ_m .

$$\delta_m = \frac{6.2897}{1.0 + 0.0097} = 6.2 \text{ inches.}$$

Use $K_1 = \frac{4102}{72} = 57 \text{ lb/in}^2$ & equation (9), set $\delta_f = 0$ and solve for δ_m .

$$\delta_m = \frac{317}{56} \sqrt{\frac{56}{57}} = 5.6 \text{ inches.}$$

Or set equation (9)=equation (16), set $\delta_f = 0$ and solve for δ_m .

$$\delta_m = \frac{6.2897}{\sqrt{\frac{5065}{4102} + 0.0097}} = 5.6 \text{ inches.}$$

The revised coefficients for 1979-82 Ford LTD's (figure 12) indicate that the first 5.7 inches of dynamic crush is completely elastic with no energy being absorbed by the vehicle's structure [use equation (1), set $\epsilon=1.0$ and solve for δ_m]. Does this correctly represent this vehicle's crush response characteristics?

In figure 13 the revised coefficients for 1981-85 Ford Escort's would indicate the first 2.5 inches of dynamic crush is completely elastic [use equation (1), set $\epsilon=1.0$ and solve for δ_m] and that a dynamic crush of 7.4 inches would occur before the onset of residual crush [use equation (9), set $\delta_r=0$ and solve for δ_m]. Can this vehicle's front end structure flex rearward through 7.4 inches with no residual damage? Wouldn't the easily damaged vehicle parts such as the fenders and hood sustain significant damaged before 7.4 inches of dynamic crush occurs? Does this correctly represent this vehicle's crush response characteristics? [Note: Equations (1) & (16) can be used to evaluate the crush-restitution relationship in the range of crush that occurs after the onset of residual crush ($\delta_r > 0$). Equation (16), however, can not be used for the initial elastic-only portion of dynamic crush (before the onset of residual crush, δ_r) since the ratio δ_r/δ_m is zero. Equation (1), therefore, must be used to evaluate the crush-restitution relationship for the dynamic crush that occurs before the onset of residual crush.]

MacInnis Engineering (SAE Paper 940916) has tested a 1981 Ford Escort. Full stroke of the front bumper isolators is 57 mm (2.25 inches). Residual crush began at a dynamic crush of 55 mm (2.17 inches). Maximum restitution of 0.61 occurred at 0.5 mm of isolator stroking (dynamic crush). The MacInnis data contradicts the revised restitution model. Restitution is not equal to a constant value of 1.0 over the first 2.5 inches of dynamic crush. In addition, the onset of residual crush occurs at a dynamic crush of 2.17 inches rather than 7.4 inches. Analysis of the revised coefficients for the 1975-79 VW Rabbit (figure 14) when compared to data from SAE Paper 940916 produce similar contradictions.

The original CRASH/SMAC programs and the revised CRASH/SMAC programs were used to estimate ΔV for a hypothetical vehicle. The authors characterize the differences (10 to 30%) between the estimated ΔV 's of the original versus revised CRASH/SMAC programs as "errors." Differences between the estimated ΔV 's would be more accurately characterized as "potential improvements in accuracy" rather than "errors." A characterization of "error" should be limited to comparisons between estimated ΔV 's and the actual ΔV 's measured during the thorough testing of a real-world vehicle.

In the Introduction section of the paper, the authors state that the original SMAC program inaccurately estimates ΔV approximately 10 to 30% for the case of direct central barrier collisions. There is no reference to the source of this information/conclusion. Hopefully this conclusion is not based upon the above "error" analysis involving hypothetical vehicles. Also in appendix 3, the authors indicate that it is "common knowledge" that the original CRASH program "underestimates the ΔV in barrier crashes by approximately 10% to 20% at 30 MPH and by greater amounts at lower speeds." Stating this is "common knowledge" should not relieve the authors of the responsibility of providing the supporting evidence for this conclusion. The lack of supporting evidence raises questions regarding the accuracy of these numbers.

The authors' revised model for restitution, although a step in the right direction, is not completely realistic. The restitution model needs to be reconfigured such that restitution is less than, or equal to, the theoretical limit of 1.0 at zero dynamic crush ($\epsilon_0 \leq 1.0$) and decreases from that point as dynamic crush increases.